




# Beyond the Standard Model

*on the lattice*

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# Current and past research

## USQCD/LQCD:

- Searching for viable technicolor theories for electroweak symmetry breaking
- Lattice supersymmetry
  - Formulations with exact SUSY
  - Use of DWF to study  $N=1$  SYM

# Technicolor – basic idea

- Dispense with elementary Higgs in SM
- Assume new (techni)-fermions carrying EW quantum numbers
- New strong force causes condensation

$$\langle \bar{Q}Q \rangle = \Lambda_{TC}^3 = O(250 \text{ GeV})^3$$

Goldstones from breaking chiral symmetries eaten to produce massive  $M_W, Z$

# Advantages

- No fine tuning Higgs mass  $m_H \sim O(\Lambda)$
- No triviality problem  $\lambda \rightarrow 0$   $\Lambda \rightarrow \infty$
- EW scale naturally small if asymptotically free

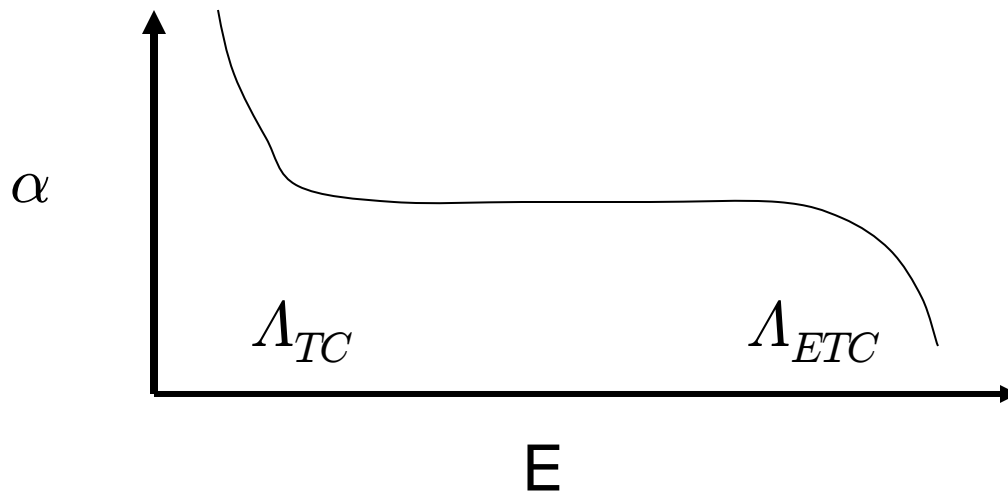
**BUT**

What gauge group, number flavors, representation ?

# Problems ...

- Scaled up QCD ( $\Lambda_{QCD} \rightarrow \Lambda_{TC}$ ) impossible
  - precision electroweak measurements at LEP would have seen it
  - To give masses to SM fermions need to couple to techniquarks in ETC theory at scale  $\Lambda_{ETC}$
  - Energies  $E < \Lambda_{ETC} \rightarrow$  4-fermion ops  $\rightarrow$  SM mass terms after techniquarks condense.
  - Absence of FCNC  $\rightarrow$  large  $\Lambda_{ETC}$  but then SM fermion masses too small ..

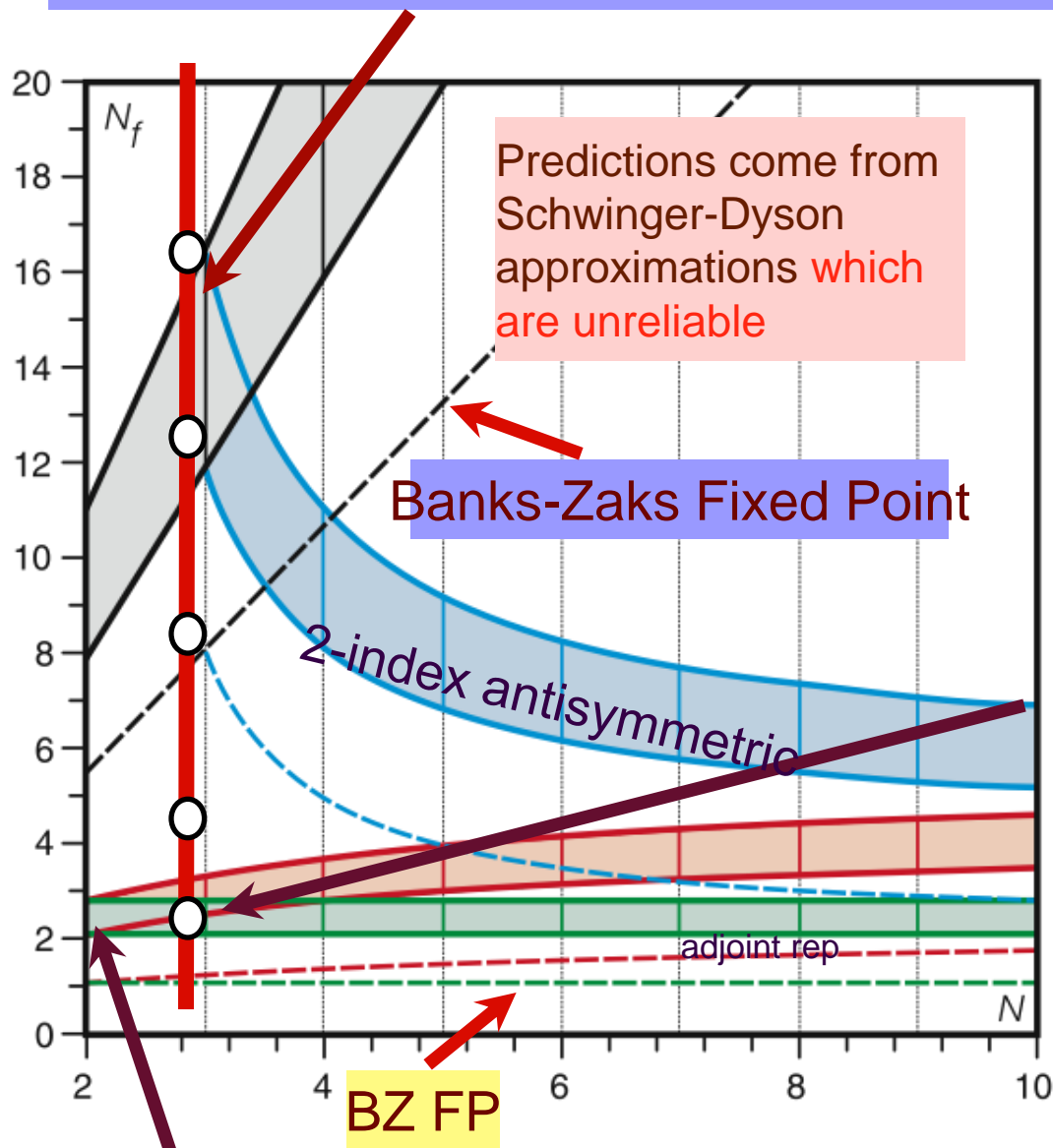
# Solution – walking dynamics



**Need to search  
theory space for  
conformal theories**

**Enhances SM fermion masses.  
Reduces contributions to S parameter  
Strongly coupled but eg spectrum  
very different to QCD**

# Theory space studied by LSD, LHC



Conformal in window  
 $N_f^1 < N_f < N_f^2$

LHC sextet model

Sannino et al 2007

MWT model  $N_f = N_c = 2$



# 3 groups within USQCD

- Syracuse/RPI/U. S. Denmark
- Lattice Strong Dynamics LSD
- Lattice Higgs Collaboration LHC



# Syracuse/RPI/Denmark

Simon Catterall, Joel Giedt, Francesco Sannino, ..

## ■ Minimal Walking Technicolor model

$$N_f=2 \text{ adj SU}(2)$$

smallest  $N_f$  for (near) conformality ?

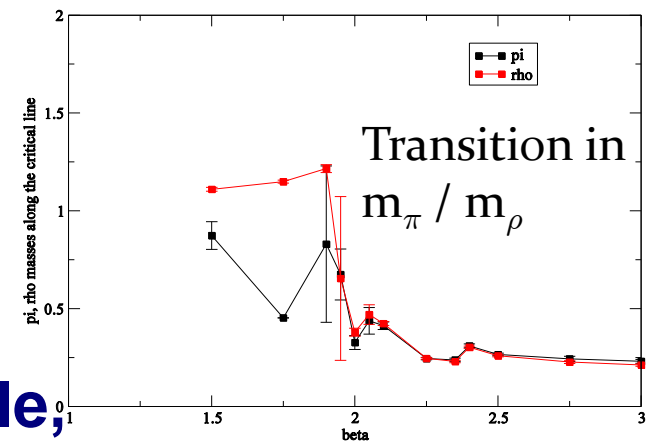
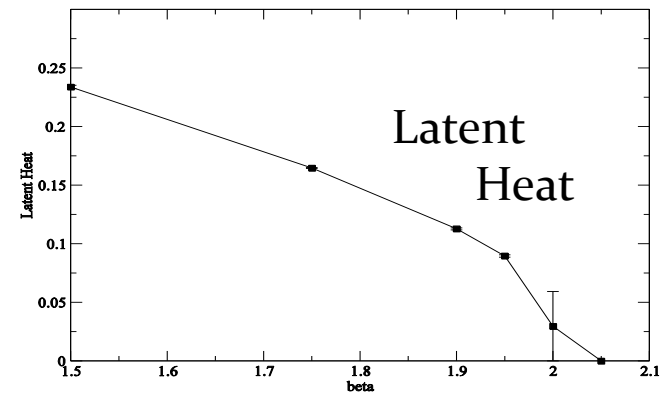
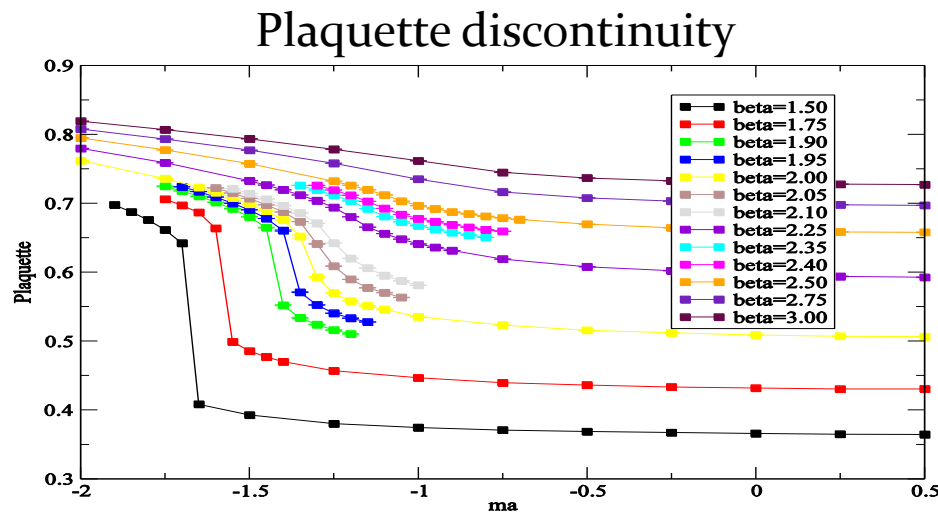
- Good place to test tools/techniques for studying such theories where **naively** need lattices  $L > 1/\Lambda$

$$\Lambda = e^{-\int \frac{dg}{\beta(g)}} \longleftarrow \text{(very) small}$$

# Minimal Walking TC

1.0 M hrs+ 0.7 M hrs BG/L

O(100) parameter pts  
 $8^3 \times 16$  Wilson



Catterall, Sannino,  
Phys.Rev.D76:034504,2007  
Catterall, Giedt, Sannino, Schneible,  
JHEP 0811:009,2008.

# Syracuse/RPI current projects

- Current  $16^3 \times 32$  clover,  $\epsilon$  -regime
  - Condensate  $\langle \bar{\psi} \psi \rangle$  function of  $m_{\text{PCAC}}$
- Exploit conformal map:  $\mathbf{R}^4 \rightarrow \mathbf{S}^3 \times \mathbf{R}$  and use finite size scaling

$$m_{\text{semi-finite geometry}} = \frac{2\pi\Delta}{L}$$

# Lattice Strong Dynamics (LSD) Collaboration

<http://www.yale.edu/LSD>



James Osborn

Ron Babich

Rich Brower

Mike Clark

Claudio Rebbi

David Schaich

Saul Cohen



Michael Cheng  
Ron Soltz  
Pavlos Vranas



Joe Kiskis



Tom Appelquist  
George Fleming  
Ethan Neil

# LSD Research Program

- Starting from QCD, study how the low energy structure varies as  $N_f$  increases towards the conformal window.
- Low energy structure includes:
  - Low energy constants of chiral perturbation theory:  $B$ ,  $F$
  - Light hadron spectrum
  - Static potential
  - Peskin-Takeuchi  $S$  parameter ( $L_{10}$  in NLO ChiPT)

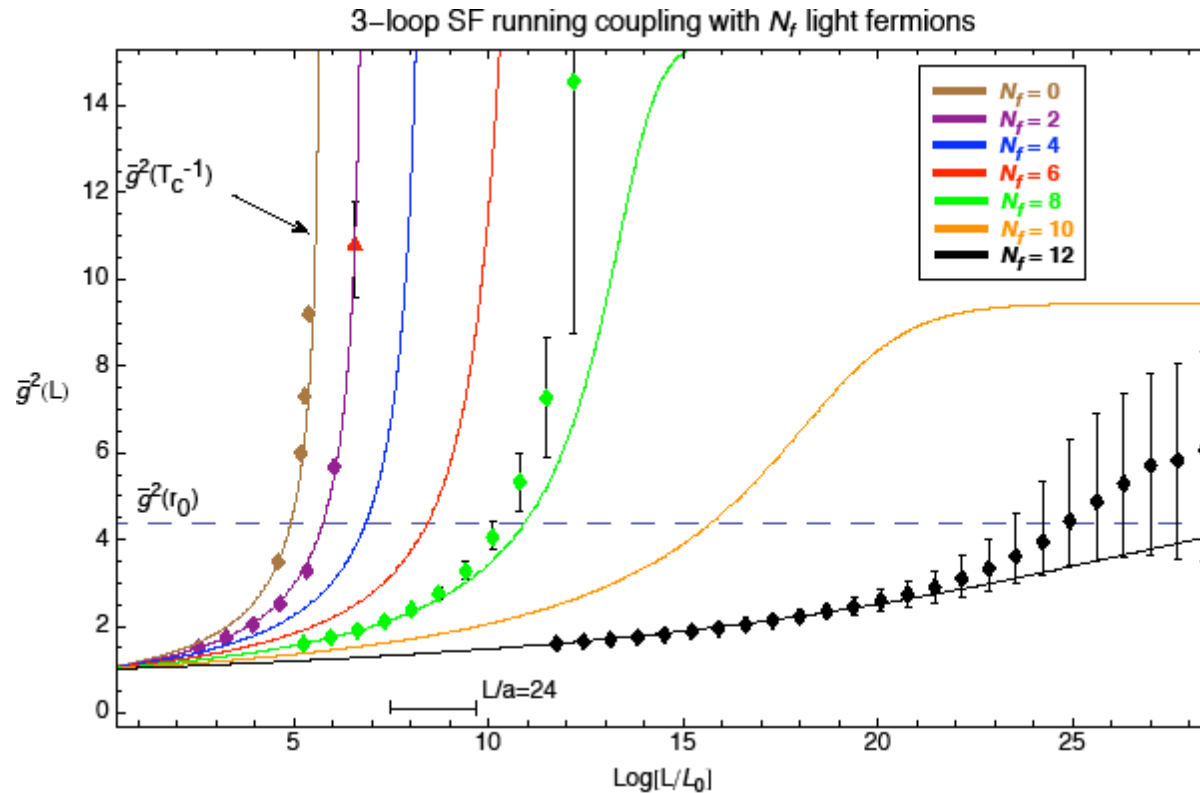
# LSD configs done

- SU(3),  $N_f=6$ ,  $24^3 \times 32$  DWF

quark mass	no. configs
0.04	480
0.0266	390
0.02	350
0.0133	355

**Currently – dedicated time on 4000 nodes QCDOC**  
**20 M node hrs**

Appelquist, Fleming, Neil, Phys. Rev. D79, 076010 (2009)  
 Phys.Rev.Lett.100:171607,2008



**Running coupling in SU(3) varying  $N_f$**

$N_f=10$  SU(3) fund. In conformal window ?

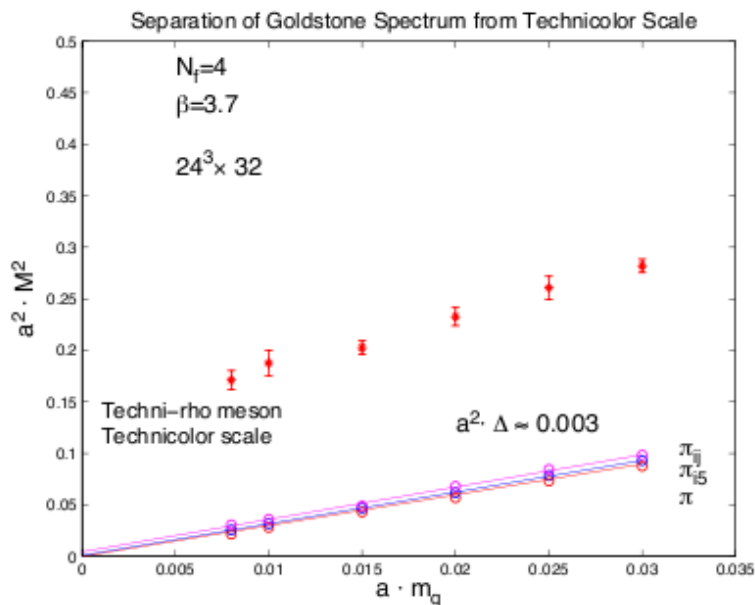
# LHC collaboration

Kuti, Fodor, Holland, Nogradi, Schroeder  
UCSD, U Pacific

## Current projects:

- SU(3) with  $N_f=2$  sextet quarks (dynamical overlap)
- SU(3) with  $N_f=4-16$  fund quarks (staggered)
  - $\epsilon$  -regime and chiral regime
- Running gauge coupling from Wilson loops
- Lattices  $16^4-28^4$ , 3.6 M hrs CPU LQCD



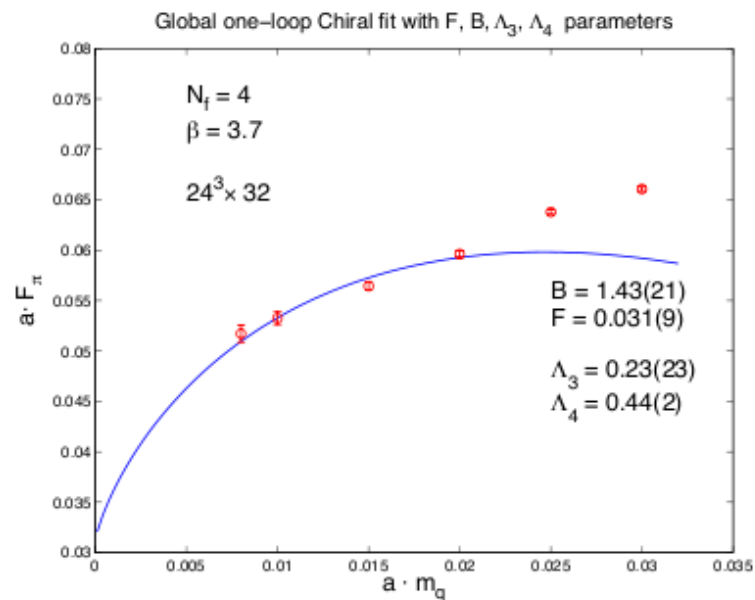
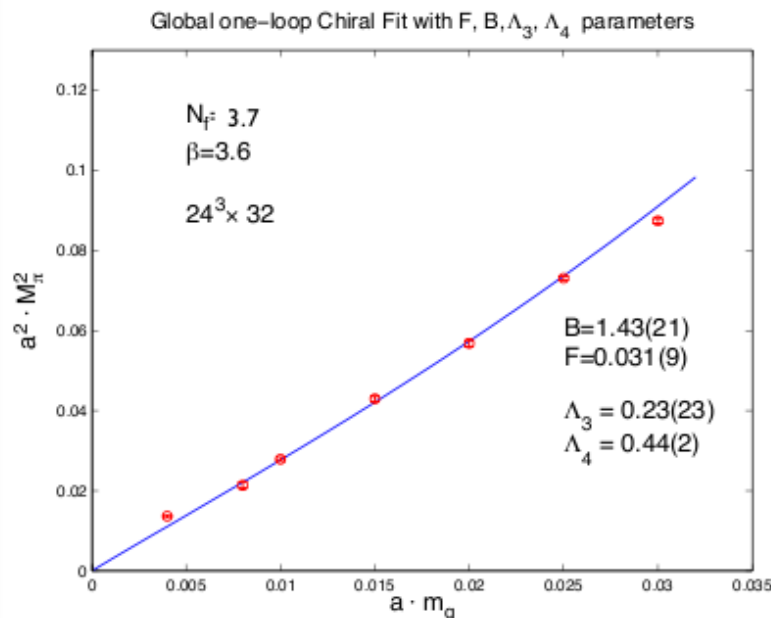


At  $\beta=3.7$  Goldstone spectrum collapses  
 Dirac eigenvalues form almost degenerate  
 quartets (this is what we want)  
 p-regime chiral loop analysis and RMT work  
 simultaneously

stringent test of chiral phase  
 $N_f=8,12$  ? We are doing it now

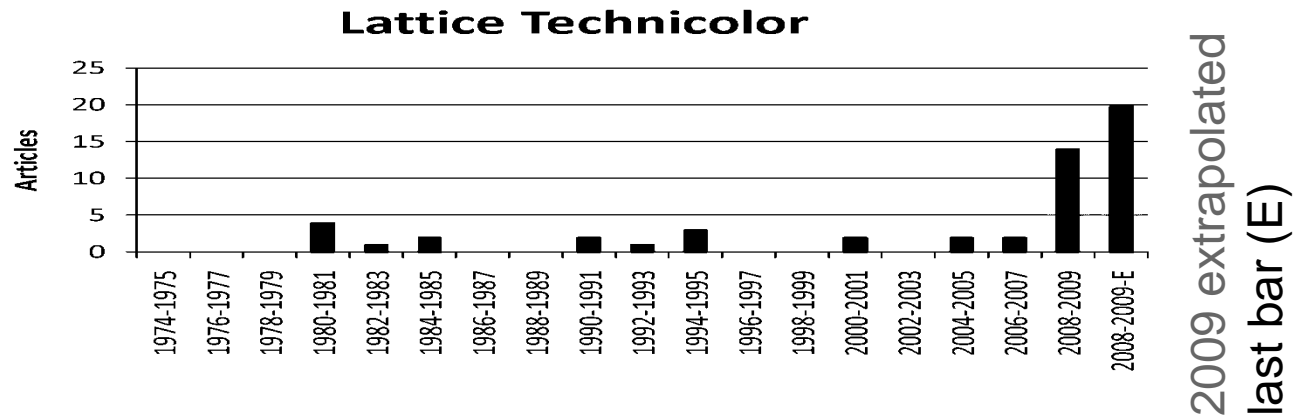
**p-regime test is increasingly difficult as  
 we approach the conformal window**

**$N_f=4$  staggered fermion (restored taste symmetry) and continuum limit reached**



# Lattice Technicolor picking up steam

**3 out of 7 groups currently active internationally in lattice technicolor are part of USQCD**



# Supersymmetry SUSY

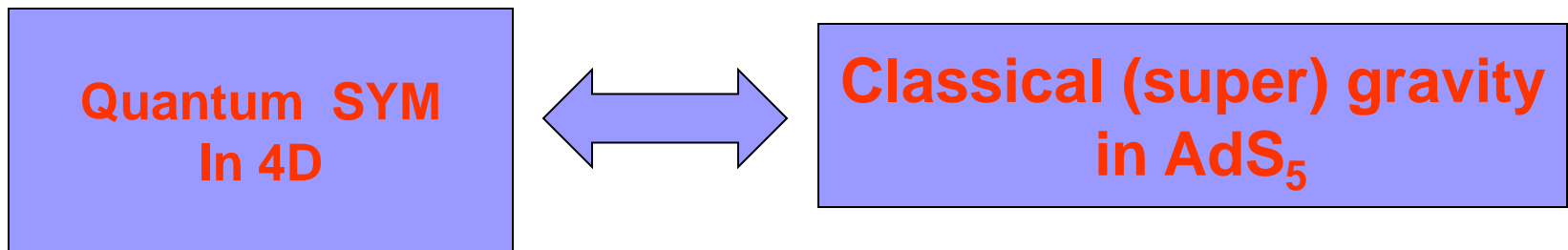
Motivations: another (popular!) extension of Standard Model:

- Higgs mass light
- Improves unification of couplings at  $M_{GUT} = O(10^{15})$  GeV
- Necessary ingredient String Theory
  - AdSCFT – quantum gravity and gauge theory

# Lattice supersymmetry

- Old hard problem. **New developments:**
  - Certain models can be discretized preserving some SUSY **exactly**
- Most interesting:  $\mathcal{N}=4$  SYM

**AdSCFT correspondence:**



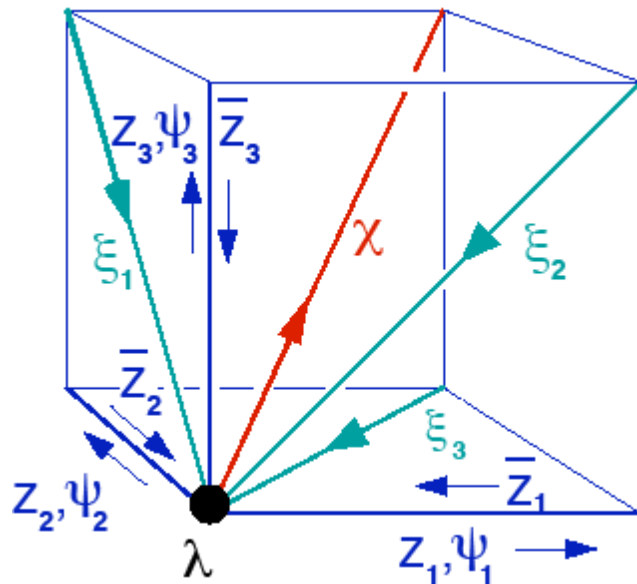
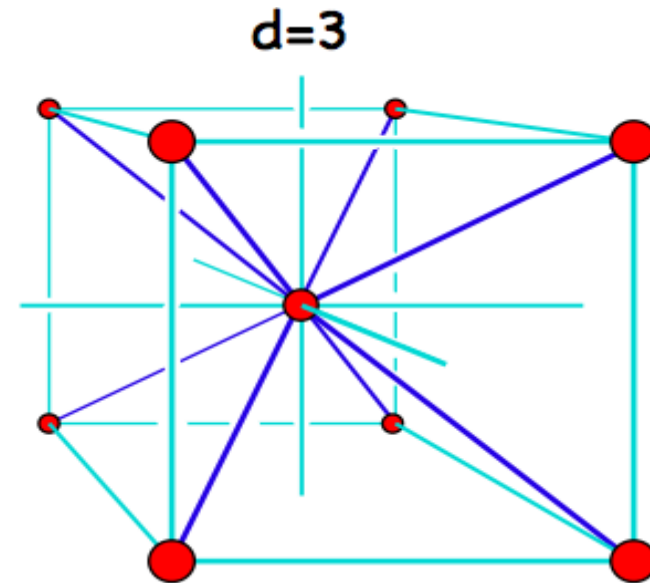
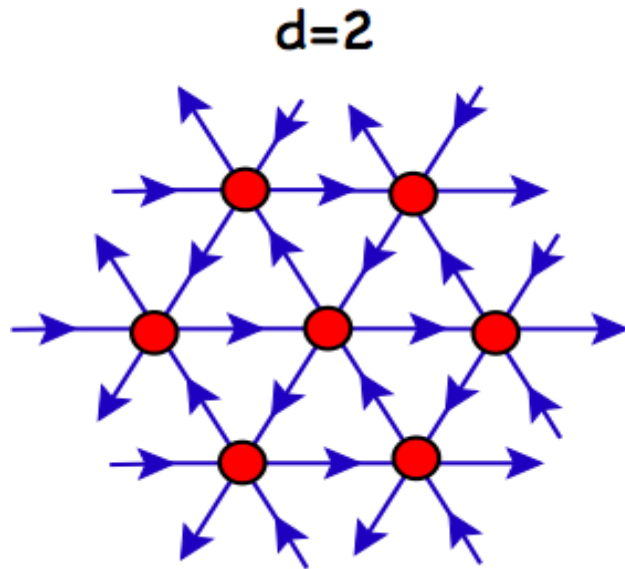
# $\mathcal{N}=4$ lattice theory

New ideas orbifolding/topological twisting

**USQCD international leadership position**

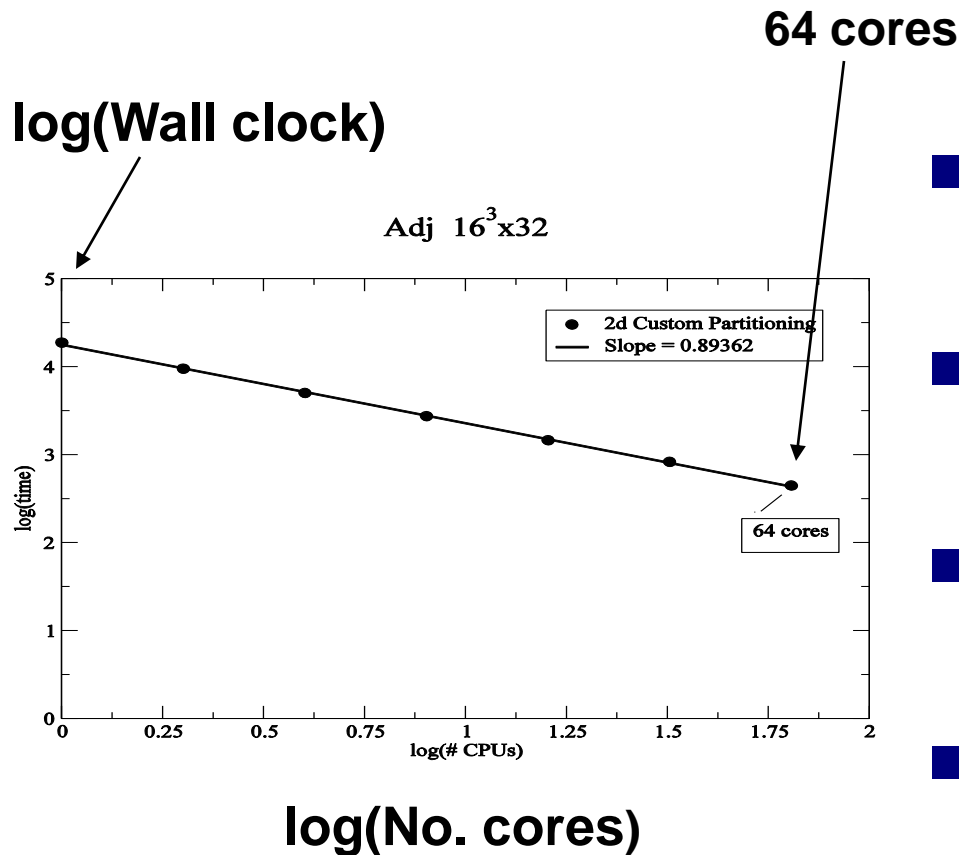
Kaplan, Catterall, Unsal **arXiv:0903.4881**,  
upcoming Phys. Rep.

Theory is local, gauge invariant,  
supersymmetric, free of doublers



**Fermions and bosons live on links.**  
**Gauge links include**  
**Scalars – complex**  
**Fermions equivalent to staggered**

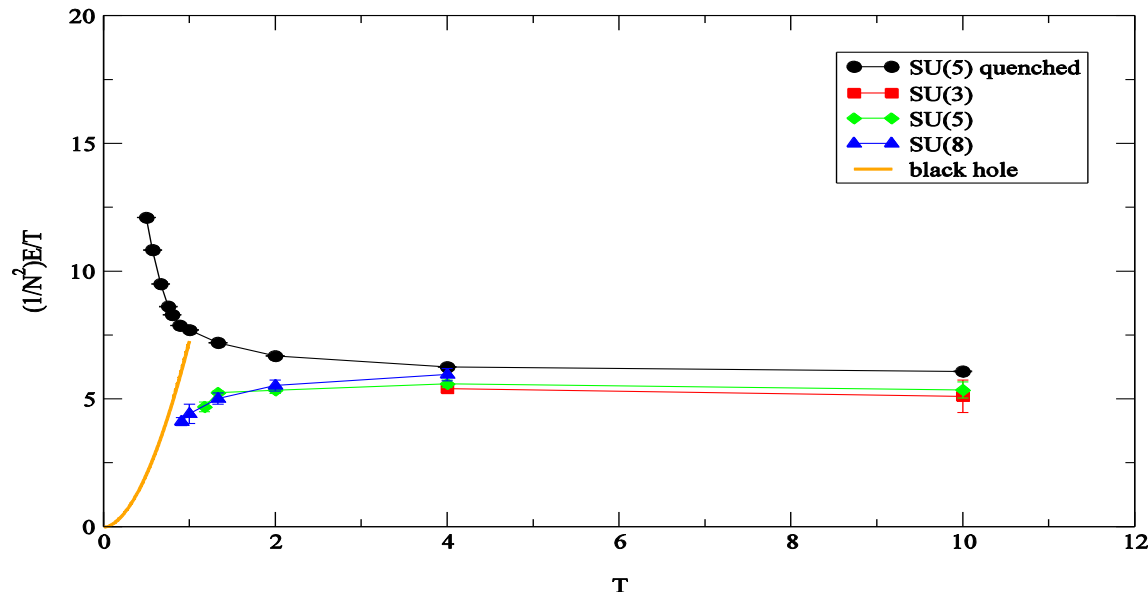
# Codes



- C++ codes written from scratch
- Use MDP libraries in FermiQCD
- Standard lattice QCD algs. eg RHMC
- Catterall  
**JHEP0901:040,2009**

# Example of AdSCFT

- SYM quantum mechanics describes black holes in  $AdS_5$



Catterall, Wiseman  
Phys.Rev.D78:041502,2008  
JHEP 0712:104,2007

0.25 M hrs LQCD



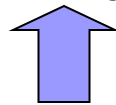
# $\mathcal{N}=4$ program

- Explore/test **AdSCFT** conjecture
  - Non BPS quantities – eg geometry impossible analytically
- Dual gauge theories **always** strongly coupled – great opportunity for lattice
  - D=2 SYM, BMN model
- Break  $\mathcal{N}=4 \rightarrow$  better route to  $\mathcal{N}=1$  ?

# $\mathcal{N}=1$ super Yang-Mills

## ■ Why ?

- Core component Minimal Supersymmetric Standard Model **MSSM**
- Stepping stone to **super QCD**  
(fermions/scalars in fundamental)



Learn about dynamical SUSY breaking,  
origin of soft breaking terms in MSSM

# DWF for $\mathcal{N}=1$ SYM

- **Cannot** use tricks to make lattice theory exactly SUSY invariant.
- However only relevant SUSY violating operator is gaugino mass
- Absent for domain wall fermions DWF

Expect SUSY restored **without** fine tuning in continuum limit

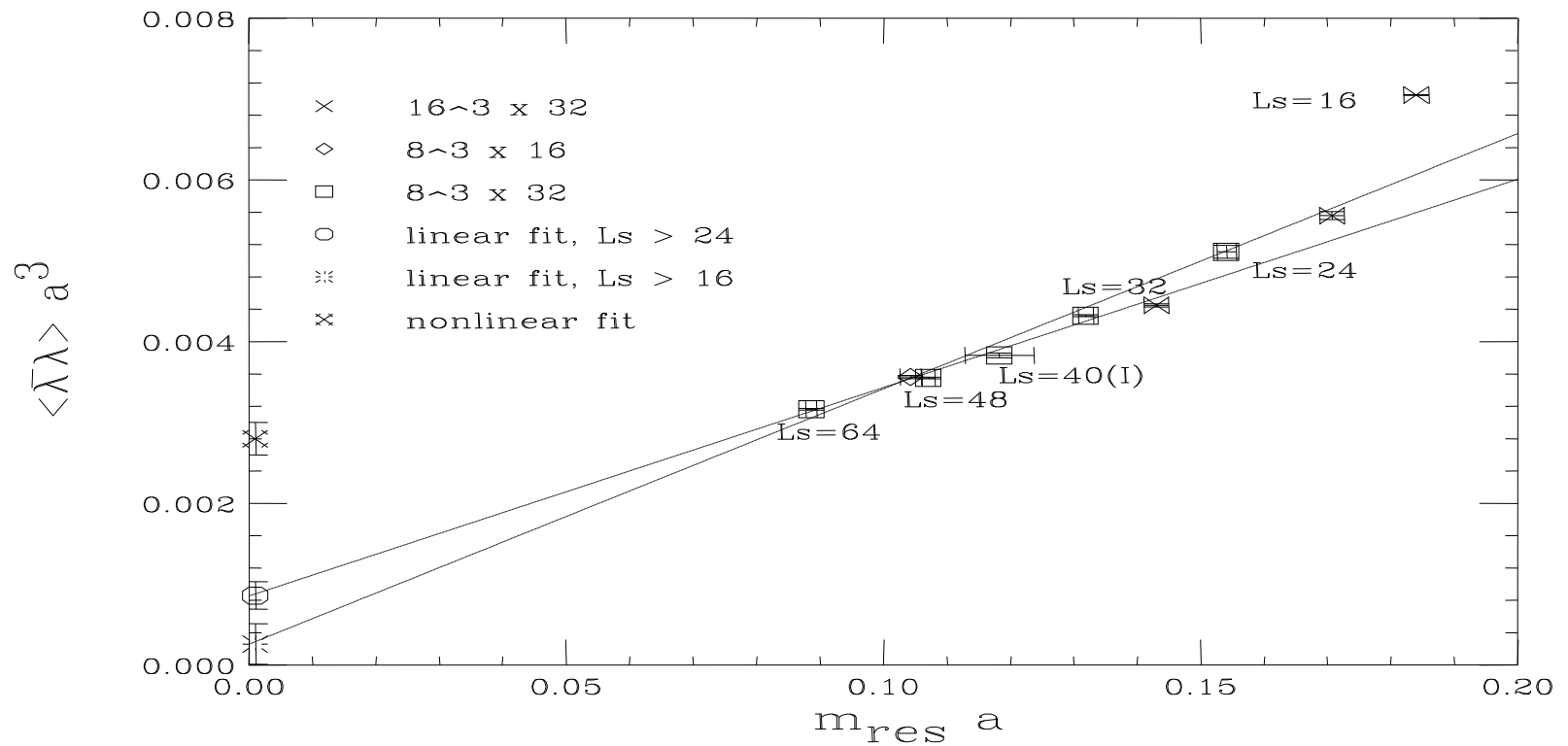
# USQCD groups:

- Endres (arXiv:0902.4267, arXiv:0810.0431)
- Giedt, Brower, Catterall, Fleming, Vranas  
(Phys.Rev.D79:025015,2009,arXiv:0807.2032)

**Gaugino condensate**

$$\langle \lambda\lambda \rangle \neq 0$$

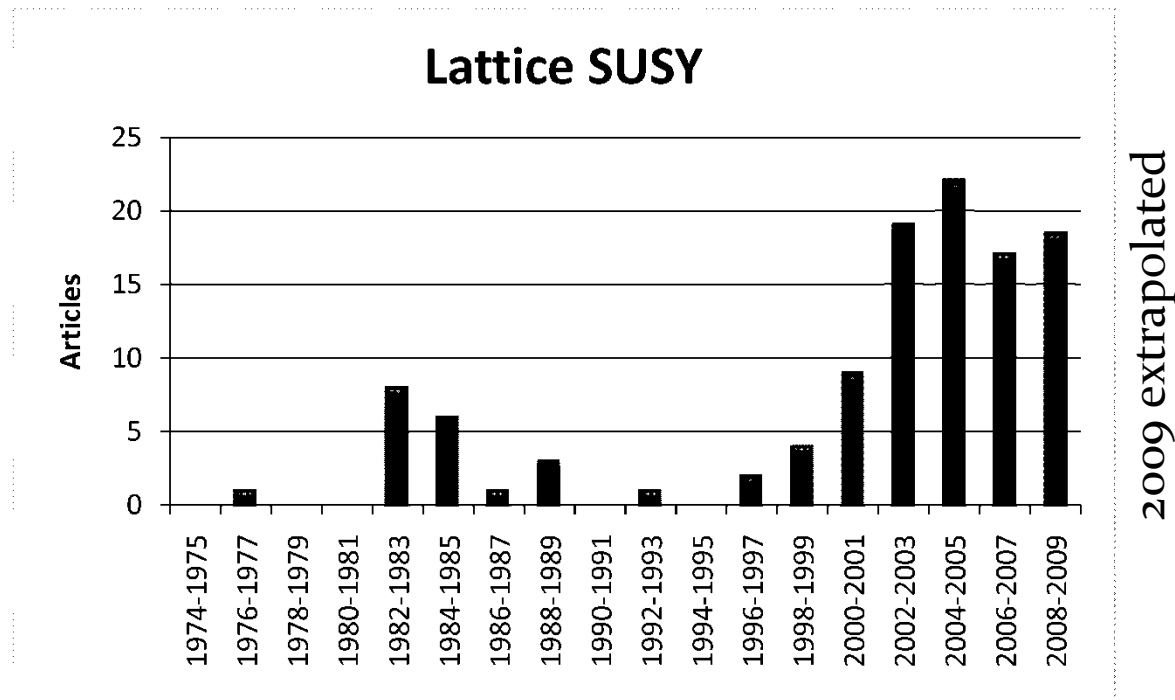
# Chiral extrapolation at $\beta=2.3$



# Program for $\mathcal{N}=1$

- Chiral limit requires  $16^3 \times 32 \times L_s$  with  $L_s > 48$ .  
40 M hrs BG/L used.
- Better implementations DWF ?
- Spectrum calcs
- Non-perturbative renormalization
- Super QCD –Need fine tune scalar sector.
  - Accomplish by reweighting. Need runs over large parameter space –  $O(100)$  harder ! – future

# Lattice SUSY: Emerging Field



# Lattice BSM and experiment

- Current mode exploratory: develop tools/experience with **non QCD** theories
- Depending on LHC → hope focus on one or two theories of most interest in near future
- TC, SUSY, or something else ? **Remain agile** ..
- Long run:
  - Employ more significant hardware resources
  - Hope to predict quantities useful to model builders eg S parameter, technihadron spectrum for TC, soft breaking terms in MSSM, ...



# Summary

## Exciting time for BSM studies on lattice!

year	percent BSM
2006-7	0.5
2007-8	4.2
2008-9	6.1
2009-10	7.1

**Excludes** 20 M hrs for N=1 SYM on BG/L and  
Comparable amount for LSD  $N_f=6$   
DWF about to start on QCDOC

- Lattice studies can provide crucial non-perturbative info on TC, SUSY, ...theories
- Current hardware/algs developed in QCD applicable.
- Exploratory and large scale simulations underway with LQCD resources